# FORM 3 TERM 3STRAND: GEOMETRYTOPIC: PolygonsKEY POINTS: concept of a polygon in concrete, representational and abstract modes; problem<br/>solving

#### **NOTES:**

A polygon with 3 sides is called a triangle

with 4 sides, a quadrilateral
with 5 sides, a pentagon
with 6 sides, a hexagon
with 7 sides, a heptagon
with 8 sides, an octagon
with 9 sides, a nonagon
with 10 sides, a decagon

#### **Properties of convex polygons:**



i) Every internal angle is less than 180° degrees

ii) With n sides, the sum of the interior angles is (2n - 4) right angles =  $(2n - 4) 90^{\circ}$  or  $(n - 2) 180^{\circ}$ 

iii) The sum of the exterior angles is  $360^{\circ}$ . At any vertex the (interior + exterior) angle =  $180^{\circ}$ 

## 1) Complete the table below:

|     | Regular Polygon | Number of | Name of  | Sum of the        | Size of    | Size of each             |
|-----|-----------------|-----------|----------|-------------------|------------|--------------------------|
|     |                 | Sides     | Polygon  | Interior          | Each       | Exterior angle           |
|     |                 |           |          | Angles            | Interior   |                          |
|     |                 | 2         |          | <b>52/2</b> 2 (2) | angle      | 2(0                      |
| a)  |                 | 3         | Triangle | [2(3) - 4)]       | 180        | 360                      |
|     |                 |           |          | $-180^{\circ}$    | 3<br>- 60° | $\frac{3}{-120^{\circ}}$ |
|     |                 |           |          | - 100             | - 00       | - 120                    |
|     |                 |           |          | or                |            |                          |
|     |                 |           |          | [3 - 2)] v        |            |                          |
|     |                 |           |          | $180^{\circ}$     |            |                          |
|     |                 |           |          | $= 180^{\circ}$   |            |                          |
| 1 \ |                 |           |          |                   |            |                          |
| b)  |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
| c)  |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     | <b>\</b> ]      |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
| d)  |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 | 10        |          |                   |            |                          |
| e)  |                 | 12        |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |
|     |                 |           |          |                   |            |                          |

2) Determine the size of the angles marked "a"



- 3) A hexagon has interior angles of 110°, 130°, 140° and 150°. If the remaining two angles are equal, then what is the size of each angle?
- 4) Determine the number of sides of a polygon in which the exterior angles of each are as follows:
  - a) 60°
  - b) 40°
  - c) 45°
  - d) 30°
  - e) 15°
- 5) Each interior angle of a regular polygon is 120°. How many sides does it have?
- 6) Each interior angle of a regular polygon is 135°. How many sides does it have?

### ANSWERS FORM 3 TERM 3 STRAND :GEOMETRY TOPIC : Polygons

**KEY POINTS** :concept of a polygon in concrete, representational and abstract modes; problem solving

1)

|    | Regular Polygon | Number of | Name of       | Sum of the    | Size of Each   |
|----|-----------------|-----------|---------------|---------------|----------------|
|    |                 | Sides     | Polygon       | Interior      | Interior       |
|    |                 |           |               | Angles        | angle          |
| a) | Λ               | 3         | Triangle      | [2(3) - 4)] x |                |
|    |                 |           |               | 90            | 180            |
|    |                 |           |               | = 180°        | 3              |
|    |                 |           |               |               | $= 60^{\circ}$ |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
| b) |                 | 4         | Quadrilateral | 360°          | 90°            |
|    |                 |           | (rectangle)   |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               | <b>5</b> 400  | 1000           |
| c) |                 | 5         | Pentagon      | 540°          | 108°           |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
| d) |                 | 6         | Hexagon       | 720°          | 120°           |
| ,  |                 |           | C             |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
| e) |                 | 12        | Dodecagon     | 1800°         | 150°           |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
|    |                 |           |               |               |                |
| 1  |                 |           | 1             | 1             |                |

- 2) a= 50°
- 3) Each angle=  $95^{\circ}$
- 4) a) 6
  - b) 9
  - c) 8
  - d) 12
  - e) 24
- 5) Polygon has 6 sides
- 6) Polygon has 8 sides